

EXPERIMENTAL ECONOMICS

DECISION-MAKING UNDER RISK

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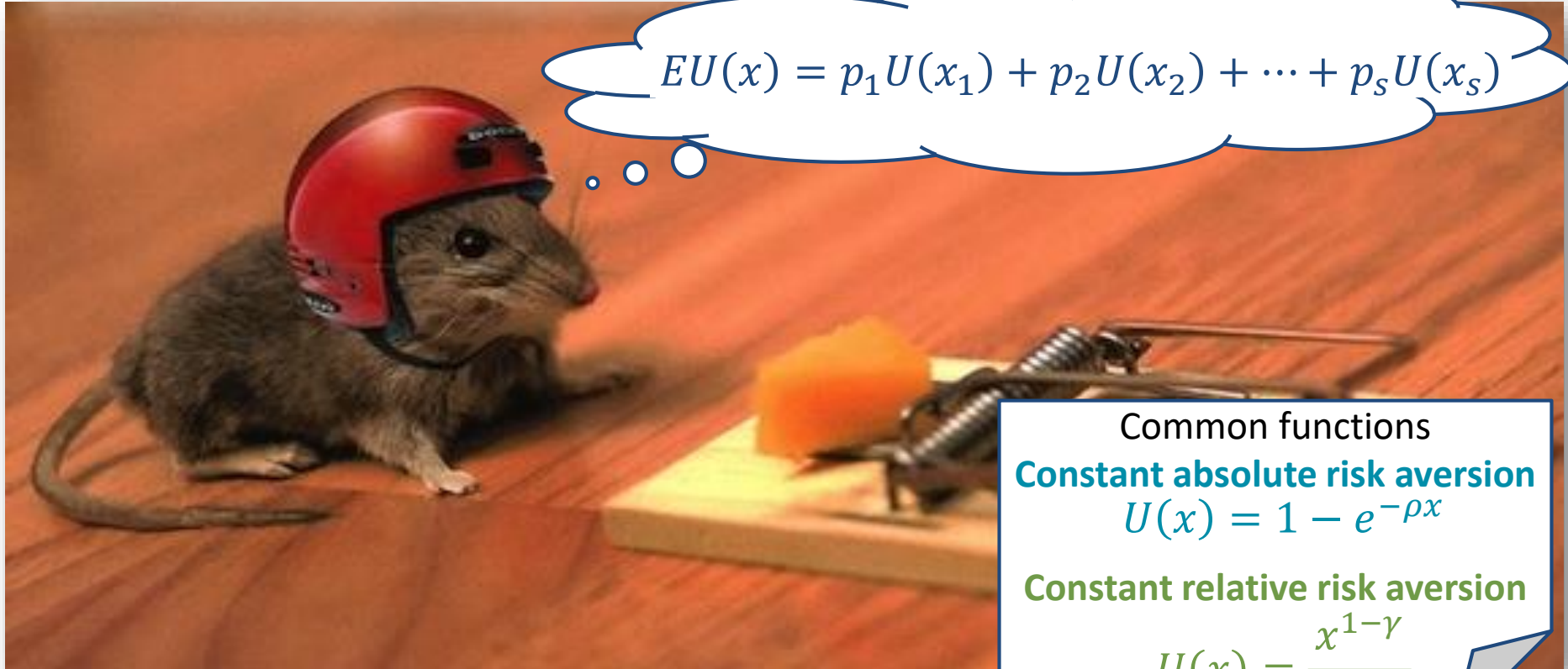
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THE ECONOMICS OF RISK AVERSION



$$EU(x) = p_1U(x_1) + p_2U(x_2) + \dots + p_sU(x_s)$$



Common functions

Constant absolute risk aversion

$$U(x) = 1 - e^{-\rho x}$$

Constant relative risk aversion

$$U(x) = \frac{x^{1-\gamma}}{1-\gamma}$$

HOW TO ELICIT RISK PREFERENCES?



Holt & Laury (2002)

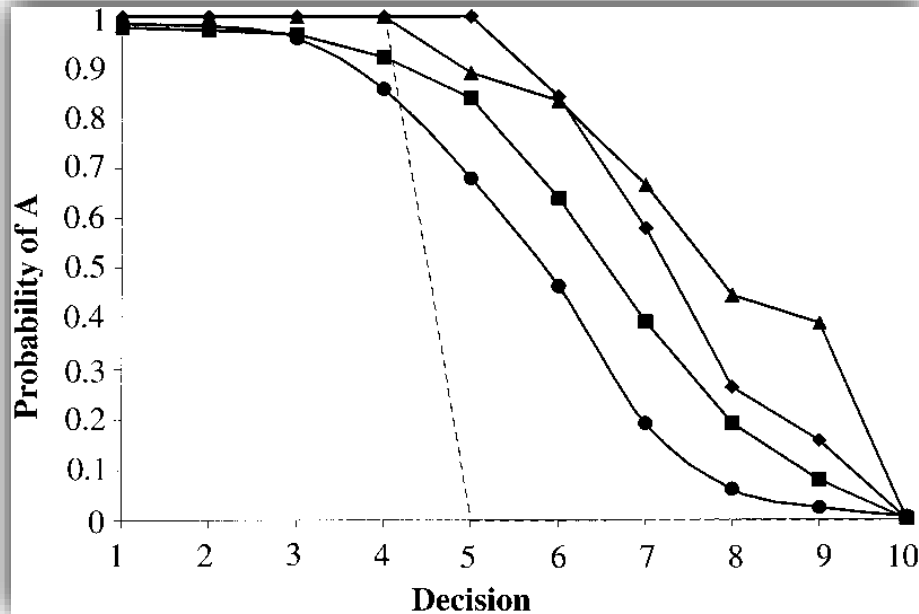
- 212 subjects choose between a series of lotteries
- Treatments: **Low** (\approx \$2.50) vs. **High** (from 20x to 90x more) vs. **High hypothetical**

Option A	Option B	Expected difference
1/10 of \$180, 9/10 of \$144	1/10 of \$347, 9/10 of \$9	\$105
2/10 of \$180, 8/10 of \$144	2/10 of \$347, 8/10 of \$9	\$75
3/10 of \$180, 7/10 of \$144	3/10 of \$347, 7/10 of \$9	\$44
4/10 of \$180, 6/10 of \$144	4/10 of \$347, 6/10 of \$9	\$14
5/10 of \$180, 5/10 of \$144	5/10 of \$347, 5/10 of \$9	(\$16)
6/10 of \$180, 4/10 of \$144	6/10 of \$347, 4/10 of \$9	(\$46)
7/10 of \$180, 3/10 of \$144	7/10 of \$347, 3/10 of \$9	(\$76)
8/10 of \$180, 2/10 of \$144	8/10 of \$347, 2/10 of \$9	(\$107)
9/10 of \$180, 1/10 of \$144	9/10 of \$347, 1/10 of \$9	(\$137)
10/10 of \$180, 0/10 of \$144	10/10 of \$347, 0/10 of \$9	(\$167)

HOW TO ELICIT RISK PREFERENCES?



Holt & Laury (2002)



Results

- Almost no risk lovers 8%
- A few risk neutral 26%
- Most are risk-averse 66%
- No difference between **Low** and **High hypothetical**
- Clear difference between **Low** and **High**
 - More risk aversion → 81%

How do they explain increasing relative risk aversion?

- Hybrid of CRRA and CARA with noisy decision making

COMPLEX VS. SIMPLE RISK-PREFERENCE ELICITATION



Dave et al. (2010)

- 881 subjects choose between a series of lotteries
- Treatments: **Simple** (Eckel & Grossman 2002) vs. **complex** (Holt & Laury 2002)

Lottery	Chose A, B, C, D, E, or F
A	1/2 of \$70, 1/2 of \$2
B	1/2 of \$60, 1/2 of \$12
C	1/2 of \$52, 1/2 of \$16
D	1/2 of \$44, 1/2 of \$20
E	1/2 of \$36, 1/2 of \$24
F	1/2 of \$28, 1/2 of \$28

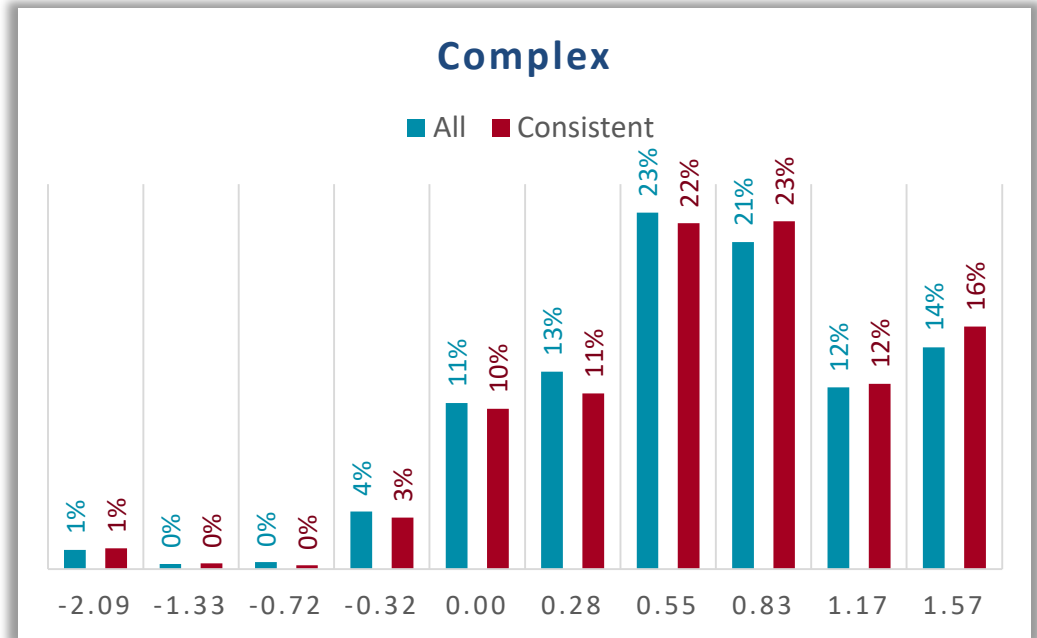
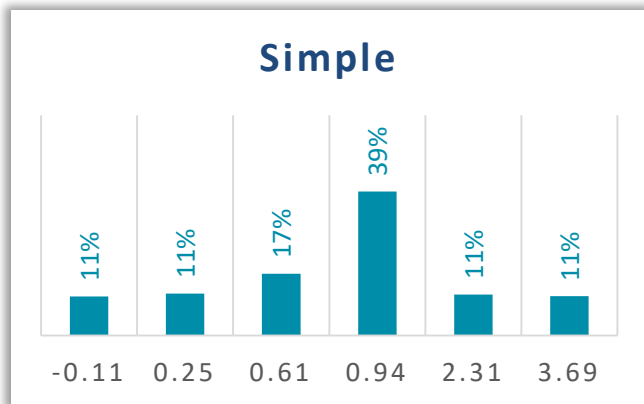
Row	Choose A or B in each row	
	A	B
1	1/10 of \$40, 9/10 of \$32	1/10 of \$77, 9/10 of \$2
2	2/10 of \$40, 8/10 of \$32	2/10 of \$77, 8/10 of \$2
3	3/10 of \$40, 7/10 of \$32	3/10 of \$77, 7/10 of \$2
4	4/10 of \$40, 6/10 of \$32	4/10 of \$77, 6/10 of \$2
5	5/10 of \$40, 5/10 of \$32	5/10 of \$77, 5/10 of \$2
6	6/10 of \$40, 4/10 of \$32	6/10 of \$77, 4/10 of \$2
7	7/10 of \$40, 3/10 of \$32	7/10 of \$77, 3/10 of \$2
8	8/10 of \$40, 2/10 of \$32	8/10 of \$77, 2/10 of \$2
9	9/10 of \$40, 1/10 of \$32	9/10 of \$77, 1/10 of \$2
10	10/10 of \$40, 0/10 of \$32	10/10 of \$77, 0/10 of \$2

COMPLEX VS. SIMPLE RISK-PREFERENCE ELICITATION



Dave et al. (2010)

- Again, mostly risk-averse 66% but different estimates depending on the technique:
Complex detects more risk aversion

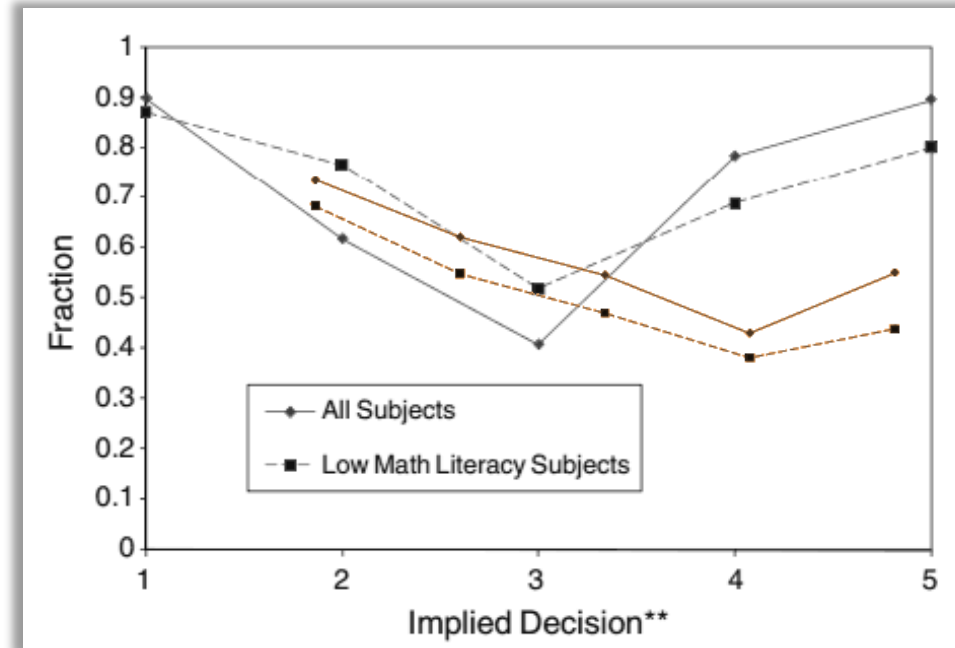


COMPLEX VS. SIMPLE RISK-PREFERENCE ELICITATION



Dave et al. (2010)

- Predictive accuracy of estimated coefficients by demographics
 - With all subjects, **Complex** has a higher predictive accuracy
 - With low-math literacy subjects, **Simple** has a higher predictive accuracy

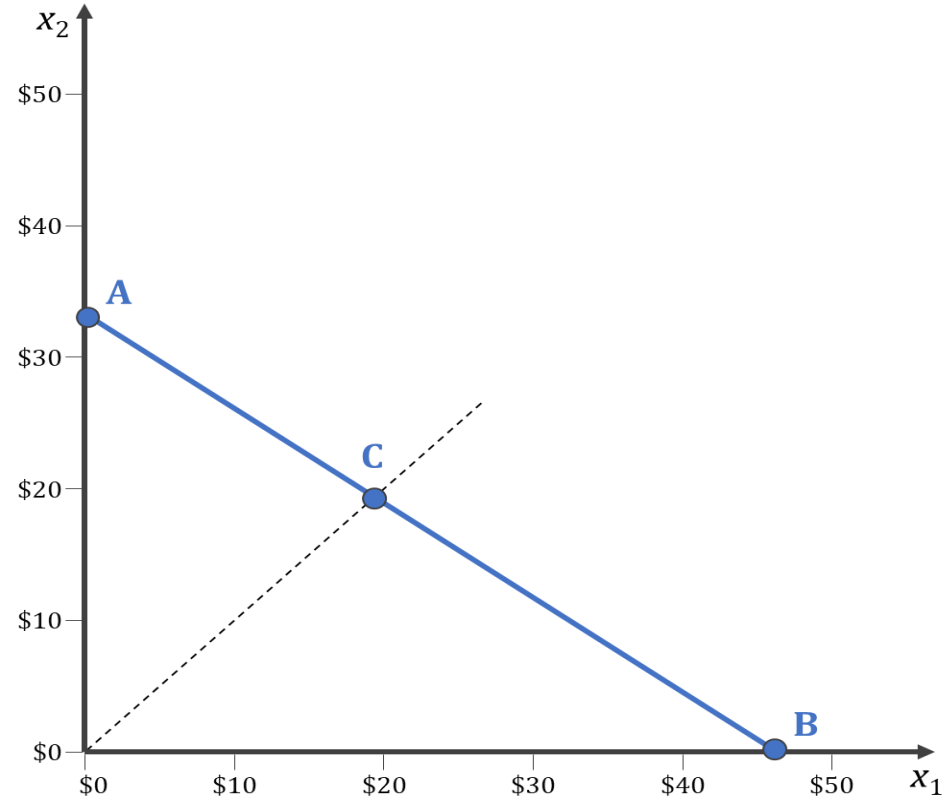


UTILITY MAXIMIZATION AND RISK-PREFERENCE ELICITATION



Choi et al. (2007)

- 93 subjects select 50 portfolios, each corresponding to a point in a budget constraint $p_1x_1 + p_2x_2 = W$, where W is their wealth and x_i is their investment in security i , which pays with probability π_i and is priced at p_i
- Choices made with a graphical interface

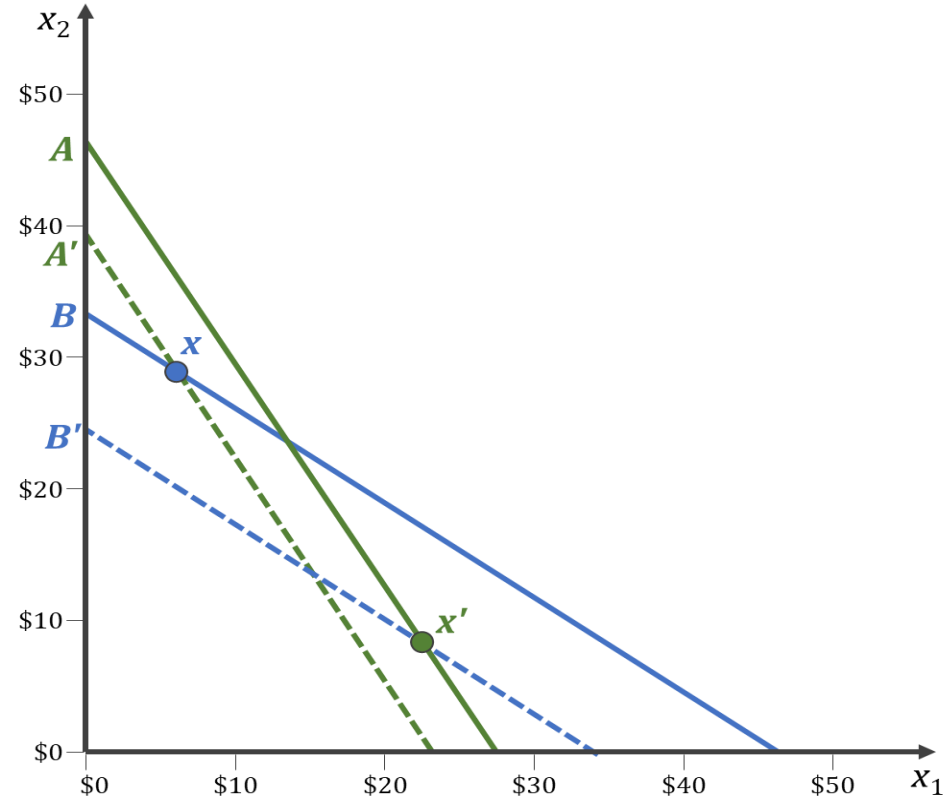


UTILITY MAXIMIZATION AND RISK-PREFERENCE ELICITATION



Choi et al. (2007)

- Measure consistency with utility maximization using the **critical cost efficiency index** (CCEI) of **Afriat (1972)**
- Minimum amount by which one has to modify budget constraints to eliminate all GARP violations



UTILITY MAXIMIZATION AND RISK-PREFERENCE ELICITATION

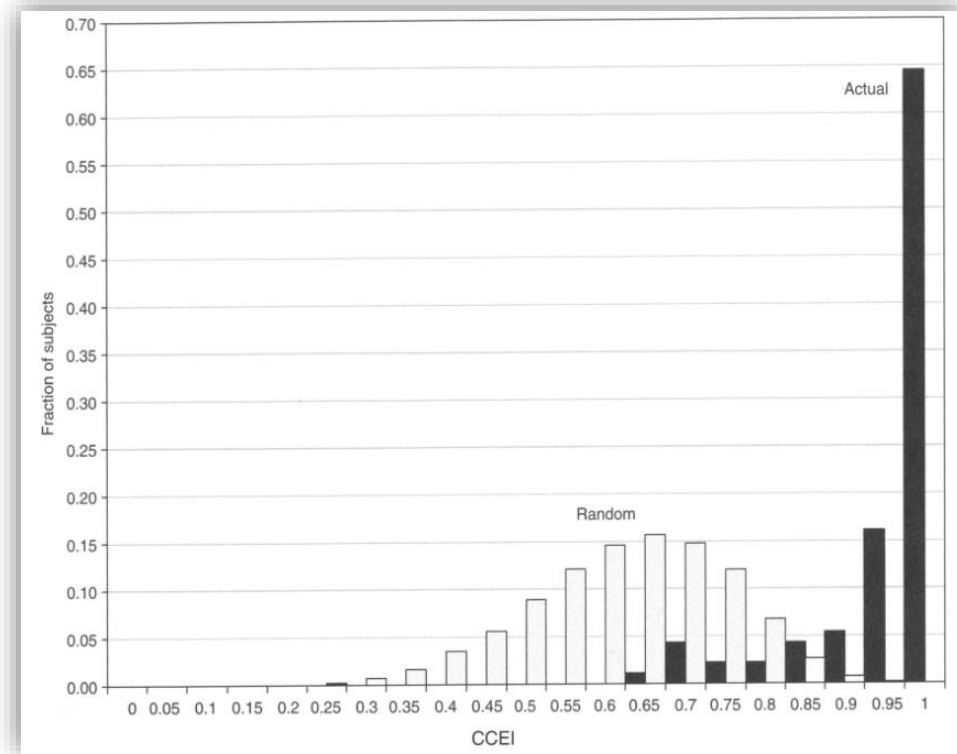


Choi et al. (2007)

- High levels of consistency with utility maximization: 80 percent have a CCEI of 0.95 or more
- Similar risk aversion coefficient estimates to other methodologies

Choi et al. (2014)

- No correlation between estimated risk aversion coefficients and CCEI
- CCEI correlates positively with income, household wealth, education, and being male and negatively with age



NON-PARAMETRIC ELICITATION OF UTILITY FUNCTIONS



van de Kuilen & Wakker (2011)

- Find the value x_1 that makes you indifferent between **A** and **B**

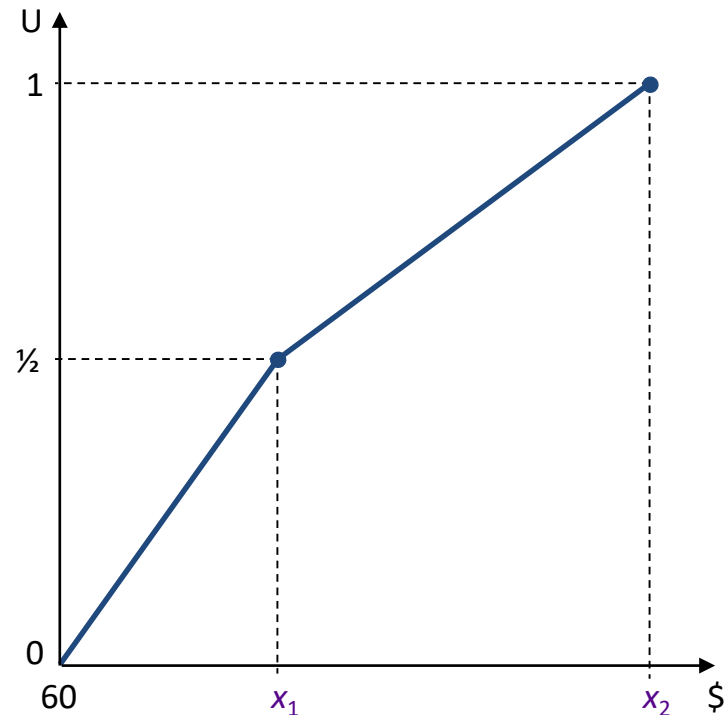


- Find the value x_2 that makes you indifferent between **C** and **D**



- etc.

Note that
 $U(x_2) - U(x_1) = U(x_1) - U(\$60)$



SMALL-STAKE RISK AVERSION



What are we eliciting with small-stake experiments? **(Rabin 2000)**

- Assume your wealth is \$1,000. Do you accept this lottery? Example with $U(x) = x^{(1-\gamma)}/(1-\gamma)$

$$\frac{1}{2} \times \$980^{(1-\gamma)}/(1-\gamma) + \frac{1}{2} \times \$1,021^{(1-\gamma)}/(1-\gamma) < \$1,000^{(1-\gamma)}/(1-\gamma) \rightarrow \gamma > 2.38091$$

- What about the following lotteries?

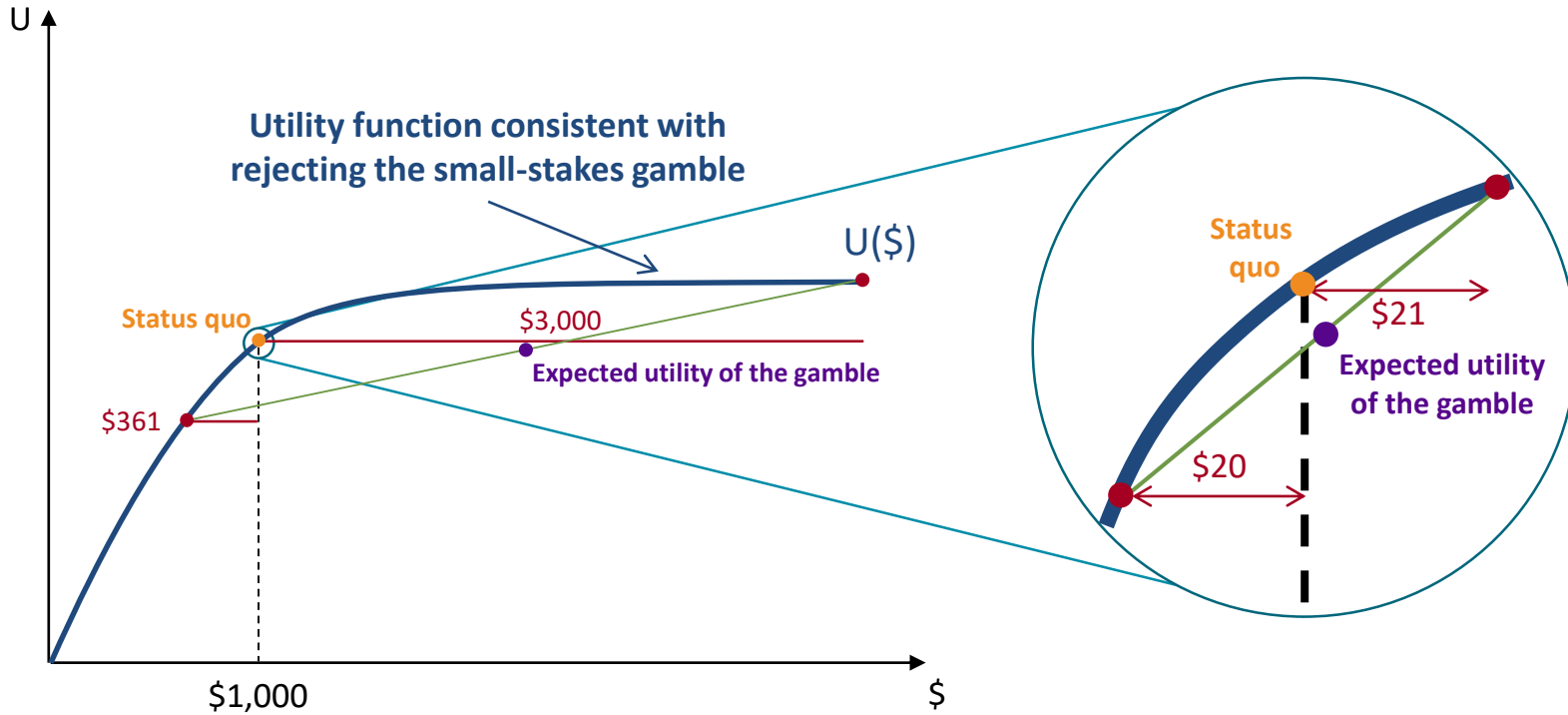
$$\frac{1}{2} \times \$843^{(1-\gamma)} + \frac{1}{2} \times \$1,250^{(1-\gamma)} < \$1,000^{(1-\gamma)}/(1-\gamma)$$

$$\frac{1}{2} \times \$732^{(1-\gamma)} + \frac{1}{2} \times \$1,750^{(1-\gamma)} < \$1,000^{(1-\gamma)}/(1-\gamma)$$

$$\frac{1}{2} \times \$639^{(1-\gamma)} + \frac{1}{2} \times \$4,000^{(1-\gamma)} < \$1,000^{(1-\gamma)}/(1-\gamma)$$

$$\frac{1}{2} \times \$605^{(1-\gamma)} + \frac{1}{2} \times \$301,000^{(1-\gamma)} < \$1,000^{(1-\gamma)}/(1-\gamma)$$

SMALL-STAKES RISK AVERSION?



SMALL-STAKE RISK AVERSION



What are we eliciting with small-stake experiments? **(Rabin 2000)**

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$$\frac{1}{2} \times \$980^{(1-\gamma)}/(1-\gamma) + \frac{1}{2} \times \$1,021^{(1-\gamma)}/(1-\gamma) < \$1,000^{(1-\gamma)}/(1-\gamma) \rightarrow \gamma > 2.38091$$

- What about the following lotteries?

$$\frac{1}{2} \times \$843^{(1-\gamma)} + \frac{1}{2} \times \$1,250^{(1-\gamma)} < \$1,000^{(1-\gamma)}/(1-\gamma)$$

$$\frac{1}{2} \times \$732^{(1-\gamma)} + \frac{1}{2} \times \$1,750^{(1-\gamma)} < \$1,000^{(1-\gamma)}/(1-\gamma)$$

$$\frac{1}{2} \times \$639^{(1-\gamma)} + \frac{1}{2} \times \$4,000^{(1-\gamma)} < \$1,000^{(1-\gamma)}/(1-\gamma)$$

$$\frac{1}{2} \times \$605^{(1-\gamma)} + \frac{1}{2} \times \$301,000^{(1-\gamma)} < \$1,000^{(1-\gamma)}/(1-\gamma)$$

- “[Loss aversion] is a departure from expected-utility theory that provides a direct explanation for modest-scale risk aversion” **(Rabin 2000)**

LOSS AVERSION



“The response to losses is consistently much more intense than the response to corresponding gains.” **(Kahneman 2003)**

- Two persons get their monthly report from a broker:
 - A is told that her wealth went from \$900,000 to \$750,000.
 - B is told that her wealth went from \$200,000 to \$250,000.
 - Who is happier today?

	Lottery (50%)	Lottery (50%)	Safe option
Choice A	\$50	\$10	\$25
Choice B	\$30	-\$10	\$5

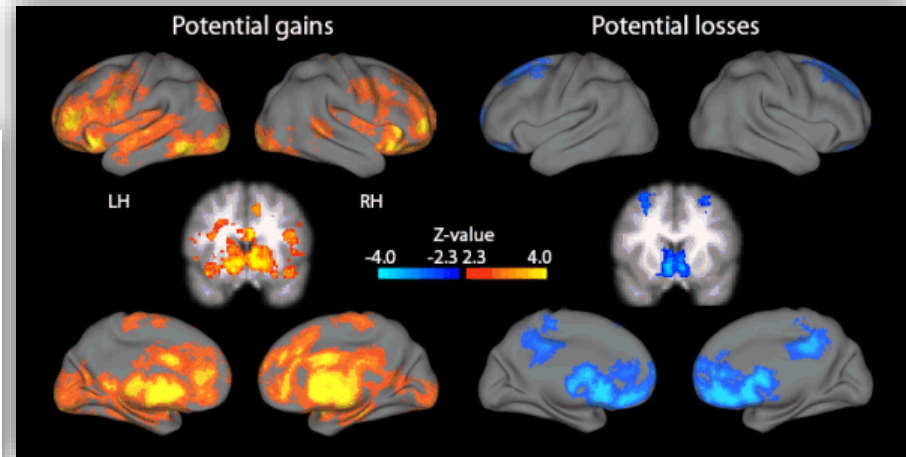
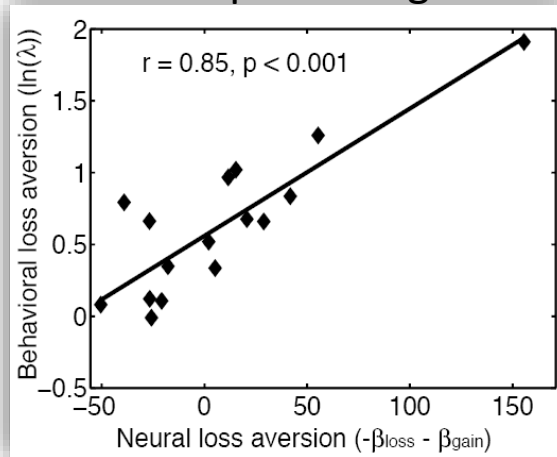
LOSS AVERSION INSIDE THE BRAIN



Can we see differences in brain activity for gains and losses? (Tom et al. 2007)

- 16 participants who accept/reject gambles while they are scanned using fMRI
- Treatments: increasing **losses** and increasing **gains**
- Activation in *ventral striatum* (associated with assignment of value)
 - Larger decrease in activation due to losses than the increase due to equivalent gains

- Difference in activation is correlated with behavioral loss aversion!



LOSS AVERSION AMONG OUR CLOSE RELATIVES



When did loss aversion evolve? Are capuchin monkeys loss averse? (Chen et al. 2006)

- First treatment (2 choices)
 - 1 apple **13%**
 - 2 apples – 0.5 × 1 apple **87%**
- Second treatment (2 choices)
 - 2 apples – 0.5 × 1 apple **29%**
 - 1 apple + 0.5 × 1 apple **71%**
- Strong preference for a gamble with gains over an equivalent gamble with a loss



MYOPIC LOSS AVERSION



Can **loss aversion** explain the **equity premium puzzle**?

- Not without additional assumptions

Myopic loss aversion (Benartzi & Thaler 1995)

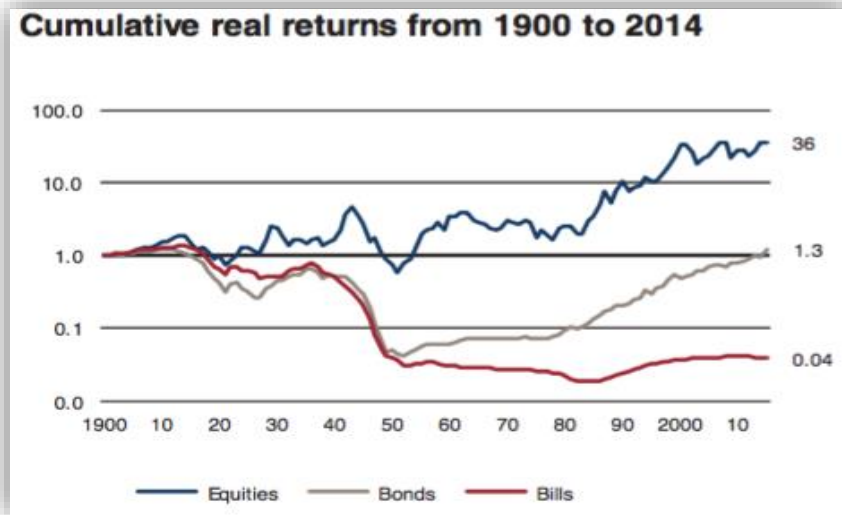
- Assume **Loss aversion** and **narrow framing**

- Would you accept this gamble?

\$50 with $p = 0.333$, $-\$20$ with $p = 0.667$

- How about this one?

\$150 with $p = 0.037$, \$80 with $p = 0.222$, \$10 with $p = 0.444$, $-\$60$ with $p = 0.297$



MYOPIC LOSS AVERSION



Gneezy & Potters (1997)

- 84 subjects bet 9 times an amount $0 \leq x \leq 200$ cents on a lottery that pays $2.5x$ with probability 33% and $-x$ with probability 67%
- Treatments: Feedback frequency is **high** (after every bet) or **low** (after every three bets)

Investment in lottery (x)	High	Low
Rounds 1-3	52.0	66.7
Rounds 4-6	44.8	63.7
Rounds 7-9	54.7	71.9
Rounds 1-9	50.5	67.4

ENDOWMENT EFFECT



“... goods that are included in the individual’s endowment will be more highly valued than those not held in the endowment, *ceteris paribus*.” (Thaler 1980)



ENDOWMENT EFFECT



Evidence of the endowment effect (List 2004)

- 124 subjects who could “trade” a candy or a mug after being **randomly-endowed** with:
- Candy** (could trade for mug), **mug** (could trade for candy), **neither** (must chose candy or mug), or **both** (must give up candy or mug)



Without experience
→

Endowed with	Ended with candy
Candy	81%
Mug	23%
Neither	45%
Both	60%

- Does market experience reduce the endowment effect? → repeat the same experiment with 129 similar subjects with market-trading experience (card dealers)

With experience
→

Endowed with	Ended with candy
Candy	47%
Mug	44%
Neither	51%
Both	44%

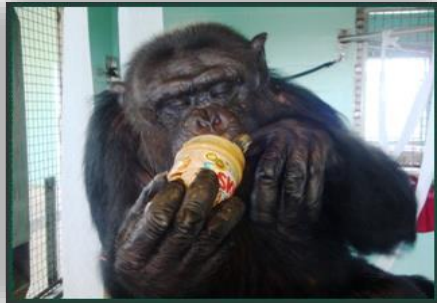
- But experience doesn't always help → card dealers exhibit more myopic loss aversion (**Haigh & List 2005**)

ENDOWMENT EFFECT AMONG OUR CLOSE RELATIVES



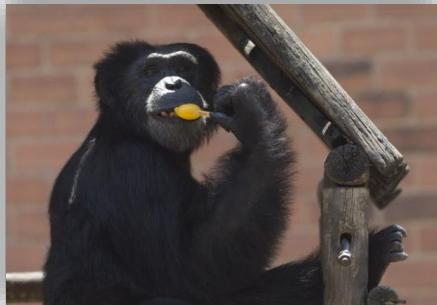
When did the endowment effect evolve? Are chimpanzees affected? (Brosnan et al. 2007)

- 33 chimpanzees chose between a **juice popsicle** or a tube of **peanut butter** either after they were randomly endowed with one of them or not



Of those not initially endowed
→ **58%** ended with **peanut butter**

Of those **endowed** with **peanut butter**
→ **79%** ended with **peanut butter**



Of those not initially endowed
→ **42%** ended with a **juice popsicle**

Of those **endowed** with **juice popsicle**
→ **58%** ended with a **juice popsicle**

EXPLAINING THE ENDOWMENT EFFECT

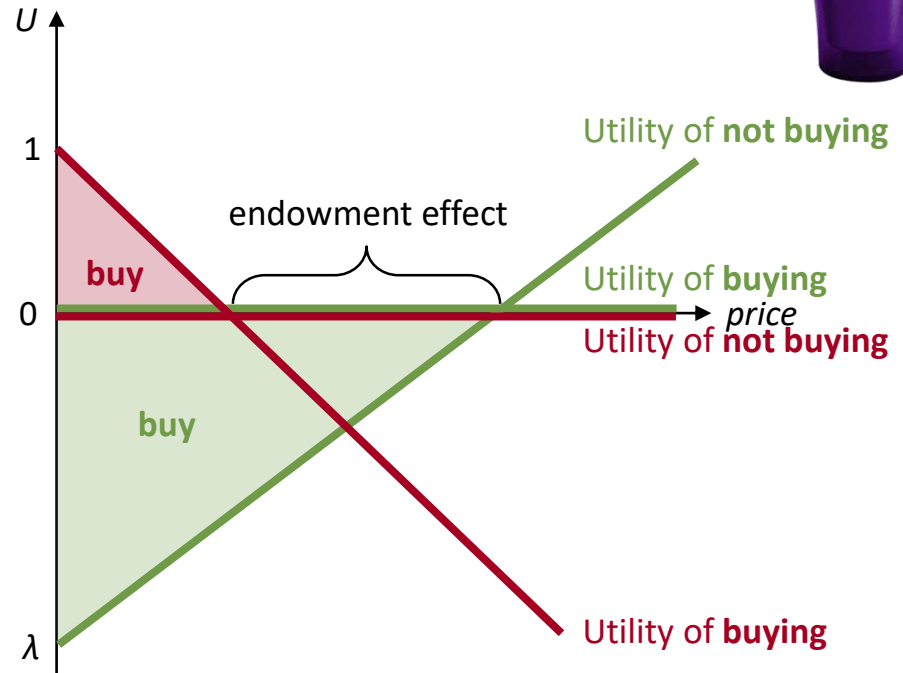


- Who just won a silver medal?
- Bronze medalists are happier because they did not expect to win (**Medvec et al. 1995**)
→ Reference-dependent risk attitudes (**Köszegi and Rabin 2007**)

EXPLAINING THE ENDOWMENT EFFECT



- Consider buying a mug
 - The utility of the mug is 1, the price is p , utility is linear in money, and losses are weighted by λ
- If your expectation is to **not buy**?
 - Utility of not buying: 0 (reference point)
 - Utility of buying: $1 - \lambda p$
- If your expectation is to **buy**?
 - Utility of buying: 0 (reference point)
 - Utility of not buying: $p - \lambda$

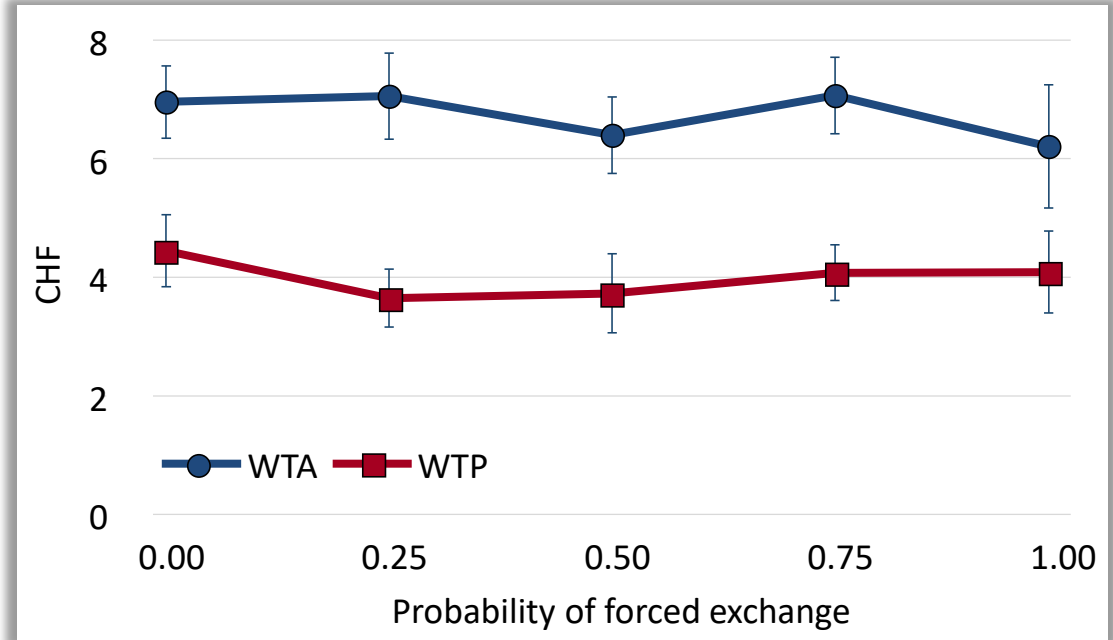


REFERENCE-DEPENDENT PREFERENCES



Reference-dependent preferences and the endowment effect (Goette et al. 2014)

- 665 subjects are endowed with either a **mug** or **10 CHF** and submit either their **WTA** or their **WTP** for the mug
- Treatments vary the probability of **forced exchange**: either **0%, 25%, 50%, 75%,** or **99%**



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